

## A general framework for animal density estimation from acoustic detections across a fixed microphone array

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### Summary

1. Acoustic monitoring can be an efficient, cheap, non-invasive alternative to physical trapping of individuals. Spatially explicit capture–recapture (SECR) methods have been proposed to estimate calling animal abundance and density from data collected by a fixed array of microphones. However, these methods make some assumptions that are unlikely to hold in many situations, and the consequences of violating these are yet to be investigated.
2. We generalize existing acoustic SECR methodology, enabling these methods to be used in a much wider variety of situations. We incorporate time-of-arrival (TOA) data collected by the microphone array, increasing the precision of calling animal density estimates. We use our method to estimate calling male density of the Cape Peninsula Moss Frog *Arthroleptella lightfooti*.
3. Our method gives rise to an estimator of calling animal density that has negligible bias, and 95% confidence intervals with appropriate coverage. We show that using TOA information can substantially improve estimate precision.
4. Our analysis of the *A. lightfooti* data provides the first statistically rigorous estimate of calling male density for an anuran population using a microphone array. This method fills a methodological gap in the monitoring of frog populations and is applicable to acoustic monitoring of other species that call or vocalize.

**Key-words:** anura, bootstrap, frog advertisement call, maximum likelihood, Pyxicephalidae, spatially explicit capture–recapture, time of arrival

### Introduction

Population size is one of the most important variables in ecology and a critical factor for conservation decision-making. Distance sampling and capture–recapture are both well-established methods used for the estimation of animal abundance and density. Both approaches calculate estimates of detection probabilities, and these provide information about how many animals in the survey area were undetected. Estimates of abundance and density are then straightforward to calculate. One particular point of difference is that distance sampling uses locations of detected individuals in *space*, while typically capture–recapture records the initial capture, and subsequent recaptures, of individuals at various points in *time*. The relatively recent introduction of spatially explicit capture–recapture (SECR) methods (Efford 2004; Borchers & Efford 2008; Royle & Young 2008; Royle *et al.* 2013; see Borchers 2012; for a non-technical overview) has married the spatial component of distance sampling and the temporal nature of capture–

recapture approaches. Indeed, Borchers *et al.* (in press) linked the two under a unifying model to show that they exist at opposite ends of a spectrum of methods, which vary with the amount of spatial information employed.

Data collected from SECR surveys are records (known as the capture histories) of where and when each individual was detected. Detection may occur in a variety of ways, for example, by physical capture, or from visual recognition of a particular individual. SECR methods treat animal activity centres as unobserved latent variables, and the positions of detectors that did (and did not) detect a particular individual are informative about its location; an individual's activity centre is likely to be close to the detectors at which it was detected.

Efford, Dawson & Borchers (2009) first proposed the application of SECR methods to detection data collected without physically capturing the animals themselves, but from an acoustic survey using an array of microphones (see section 9.4, Royle *et al.* 2013; for a summary of acoustic SECR methods). This is appealing when the species of interest is visually cryptic and difficult to trap physically, but is acoustically detectable. Moreover, it is less disruptive and invasive than physical capture. When individuals can be detected (virtually) simulta-

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neously on multiple detectors (e.g. by virtue of the same call being recorded at multiple microphones), then ‘recaptures’ (or, more accurately, ‘redetections’) occur at different points in space rather than across time, thus removing the need for multiple survey occasions. This has the advantage of substantially reducing the cost of fieldwork. In this case, the capture histories simply indicate which microphones detected each call, and no longer have a temporal component. The latent locations are no longer considered activity centres, but simply the physical location of the individual when the call was made. The use of SECR for these data is advantageous over competing approaches (e.g. distance sampling) as these often assume that the locations can be determined without error, and this does not hold in many cases.

The method of Efford, Dawson & Borchers (2009) used signal strengths (i.e. the loudness of a received call at a microphone) to improve estimates of individuals’ locations: microphones that received a stronger signal of a particular call are likely to be closer to the latent source locations than those that received a weaker signal. Such additional information is capable of improving the precision of parameter estimates (Borchers *et al.* in press).

Naturally, acoustic detection methods are unable to estimate the density of non-calling individuals. Any density estimates obtained from acoustic surveys therefore correspond to the density of calling individuals, or density of calls themselves (i.e. calls per unit area per unit time), rather than overall population density. If the proportion of individuals in the population that call is known (or can be estimated), then it is straightforward to convert estimated calling animal density to population density. Otherwise, the utility of measures related to abundance or density (e.g. relative abundance indices) has been shown for a variety of taxa, of which only subsets of the populations are acoustically detectable.

For example, females do not call for almost all anuran species. It is therefore only possible to obtain an estimate of calling male density from an acoustic survey. Nevertheless, qualitative estimates of call density (i.e. density recorded on a categorical scale) for frog populations have been found to correlate well with capture–recapture estimates (Grafe & Meuche 2005), and male chorus participation is the best known determinant of mating success in many frog species (Halliday & Tejedo 1995). As a result, call density is often used as a proxy for frog density (e.g. Corn, Muths & Iko 2000; Crouch & Paton 2002; Pellet, Helfer & Yannic 2007).

Further examples of taxa for which measures related to abundance and density have been estimated using acoustic methods include birds (e.g. Buckland 2006; Celis-Murillo, Deppe & Allen 2009; Dawson & Efford 2009), cetaceans (e.g. Harris *et al.* 2013; Martin *et al.* 2013), insects (e.g. Fischer *et al.* 1997) and primates (e.g. Phoonjampa *et al.* 2011). See Marques *et al.* (2013) for an overview of the use of passive acoustics for the estimation of population density.

While the method of Efford, Dawson & Borchers (2009) shows promise in estimating calling animal abundance and density using fixed arrays of acoustic detectors, a major practical issue was not addressed in this work: the method as

described is only appropriate if each individual is only detectable on a single occasion (e.g. by virtue of making exactly one call). The likelihood presented assumes independent detections between calls, thus independence between call locations. This is unlikely to hold when individuals emit more than a single call, as locations of calls made by the same individual are almost certainly related. This issue was not explicitly acknowledged, and as a result, the subsequent analyses presented by Marques *et al.* (2012) and Martin *et al.* (2013), which apply the method of Efford, Dawson & Borchers (2009), are problematic. Additionally, the analysis of Dawson & Efford (2009) used an approach that is unlikely to be appropriate in many scenarios. We outline these studies below.

Marques *et al.* (2012) and Martin *et al.* (2013) applied acoustic SECR methods to data collected by underwater hydrophones, which detected vocalizations from minke whales *Balaenoptera acutorostrata* Lacépède. As the location of a whale’s call is likely to be close to the location of its previous call, this analysis suffers the assumption violation mentioned above. The consequences of this violation are not clear.

Furthermore, calls were treated as the unit of detection meaning that each call (rather than each individual) was given its own capture history. The resulting density estimate was therefore of call density rather than calling whale density. Distance sampling analyses have previously used independently estimated call rates to convert from call density to calling animal density (e.g. Buckland 2006), and Efford, Dawson & Borchers (2009) suggest using the same approach. The efficacy of this approach in an SECR setting is yet to be investigated, and a way of estimating variance of animal density estimates generated in this way has not yet been proposed.

Dawson & Efford (2009) estimated density of singing ovenbirds *Seiurus aurocapilla* (Linnaeus) using small arrays of microphones. Of all calls attributed to the same individual, only the first was retained for analysis. Assuming independence between locations of retained calls was therefore appropriate, and the resulting density estimate was of singing bird density. However, there are two potential problems with this practice: first, it can only be carried out in situations where individuals are recognizable from their calls, and on many surveys, this is not the case. Second, recall that the likelihood assumes each individual is only detectable on a single occasion. Therefore, any detections retained for analysis must be detections of the first call the individual made *over the course of the survey*, and not only the first call that was *detected*. In general, it is not known when a call is undetected, and so one cannot be sure that the first detected call is the first call. Retaining calls that were the first detected call, but not the first emitted call, can result in positive bias in calling animal density estimates.

Putting the method of Efford, Dawson & Borchers (2009) into practice is therefore problematic. It is necessary to investigate the consequences of violating assumptions of call location independence and propose suitable estimators based on acoustic detection data from a microphone array. In this manuscript we present a general method that gives rise to estimators of calling animal density. We also develop methodology that can be used to estimate variance of the proposed estimators. We

show by simulation that both perform well under reasonable assumptions.

An additional improvement is possible, which we also incorporate into our estimator. While Efford, Dawson & Borchers (2009) suggest the use of received signal strengths to further inform call locations (in addition to detection locations), Borchers *et al.* (in press) demonstrate the utility of time-of-arrival information in this regard. Multichannel arrays are capable of recording the precise times at which a signal is detected by each individual microphone, and subtle differences between these times are informative about the location of the sound source. For example, a call's source location is likely to be closest to the microphone with the earliest detection time. The use of such auxiliary data informative on call locations in acoustic SECR is further motivated by Fewster & Jupp (2013), who show that incorporating response data from additional sources leads to estimators that are asymptotically more efficient. Indeed, we show via simulation that our estimator has less bias and is more precise when it incorporates time-of-arrival data.

We use our method to estimate calling male density of the Cape Peninsula Moss Frog *Arthroleptella lightfooti* (Boulenger) from an acoustic survey. The genus *Arthroleptella* (moss frogs; family Pyxicephalidae) are tiny (adults are typically 7–8 mm total length), visually cryptic and inhabit seepages on mountain tops in South Africa's Western Cape Province (Channing 2004). Due to the region's topography, many species are severely range restricted, endemic to individual mountains, such that most of the genus are on the IUCN red list (1 Critically Endangered, 1 Vulnerable, 3 Near Threatened and 2 Least Concern; Measey 2011).

Individuals are extremely hard to find (approximately 3–4 person-hours per individual) and therefore prohibitively expensive to monitor via direct observation. However, males can be heard calling throughout the austral winter from within montane seepages, making an acoustic survey ideal. Movement of individuals is minimal over the course of such surveys; during physical searches, frogs appear to call from the same precise locations (Measey, pers. obs.). Currently, these populations are monitored with a subjective estimate of calling male abundance (Measey *et al.* 2011). Such subjective methods are typically employed in anuran monitoring methodologies (Dorcas *et al.* 2009). These estimates have no corresponding measure of estimate uncertainty. Additionally, there is no formal way of accurately determining the survey area within which individuals are detected, and so estimates of calling male density are not available. Indeed, Dorcas *et al.* (2009) conclude that current auditory monitoring approaches to surveying anuran populations are restricted in their ability to estimate abundance or density. At present, no method exists that is capable of generating both point and interval estimates of either call or calling male density in a statistically rigorous manner. For the genus *Arthroleptella* (among others), this problem is further compounded by the lack of any method capable of identifying individuals from their calls, so it is not known how many different individuals have been detected. The method we present overcomes these problems.

## Materials and methods

### OVERVIEW

Our method has three main components:

1. An acoustic SECR survey from which call density is estimated.
2. Estimation of the average call rate, allowing for conversion of the call density estimate into a calling animal density estimate.
3. A parametric bootstrap procedure for variance estimation.

Once call density is estimated in Step 1, establishing an estimate for the mean call rate in Step 2 allows for the estimation of calling animal density. Measures of parameter uncertainty (such as standard errors and confidence intervals) are calculated using a parametric bootstrap approach. Parameter estimates from both Step 1 and Step 2 are required in order to carry out this procedure.

The SECR model we present for Step 1 assumes that individual calls are identifiable, that is, it is known whether or not two detections at different microphones are of the same call. Some acoustic pre-processing is required in order to ascertain how many unique calls were detected across the array and which of these were detected by each of the microphones. The details of this process will vary from study to study depending on factors such as the acoustic properties of the focal species' calls. We later describe a simple method used for the application to *A. lightfooti*, which is suitable for our survey.

We do not assume that individuals are identifiable, that is, our method does not require knowledge of whether or not two detected calls were made by the same animal. This is more difficult than identifying calls; there is less information available from which to determine individual identification, and one must contend with between-call variation in whatever acoustic properties of the calls are measured.

### NOTATION AND TERMINOLOGY

We consider a survey of duration  $T$  with  $k$  microphones placed at known locations within the survey region  $A \subset \mathbb{R}^2$ . Vocalizations from members of the focal species are detected by these microphones, and measurements of the received signal strength and time of arrival are collected for each detection. A detection is defined to be a received acoustic signal of a call that has a strength above a particular threshold,  $c$ , so that is easily identifiable above any background noise. Detections with strengths below this threshold are discarded.

The observed data comprise the number of unique calls detected,  $n_c$ , capture histories of the detected calls,  $\Omega$ , recorded signal strengths,  $Y$ , and times of arrival measured from some reference point (typically the beginning of the survey),  $Z$ . These are defined as follows.

Let  $\omega_{ij}$  be 1 if call  $i \in \{1, \dots, n_c\}$  was detected at microphone  $j \in \{1, \dots, k\}$ , and 0 otherwise. We denote  $\omega_i = (\omega_{i1}, \dots, \omega_{ik})$  as the capture history for the  $i^{\text{th}}$  call on the  $k$  detectors, and  $\Omega$  contains the capture histories for all  $n_c$  calls. If the  $i^{\text{th}}$  call was detected by the  $j^{\text{th}}$  microphone, then we also observe  $y_{ij}$  and  $z_{ij}$ , the measured signal strength and the recorded time of arrival from the start of the survey, respectively. The sets of all these observations are given by  $Y$  and  $Z$ , and  $y_i$  and  $z_i$  contain the signal strength and time-of-arrival information associated with the  $i^{\text{th}}$  call.

The detected calls have unobserved locations  $X = (x_1, \dots, x_{n_c})$ , where  $x_i \in A$  provides the Cartesian coordinates of the location at which the  $i^{\text{th}}$  call was made. We also use  $x$  generically to denote a particular location within the survey region. Note that locations of calls emitted by the same individual cannot be considered independent. As it is

not known which calls were made by the same individual, call locations in general are not independent.

The parameter vector  $\theta=(D_c, \gamma, \phi)$  is estimated from the acoustic survey data. The scalar  $D_c$  is call density (calls per unit area per unit time), which is assumed to be constant across the survey area covered by the array (although see the discussion for comments on modelling spatial variation in calling animal and call density), while the vectors  $\gamma$  and  $\phi$  contain parameters associated with the signal strength and time-of-arrival processes, respectively.

The detection function and the effective sampling area (ESA) play important roles in both SECR and distance sampling, and so they are worth briefly introducing here. The detection function  $g(d; \gamma)$  gives the probability that a call is detected by a microphone, given that their respective locations are separated by distance  $d$ . This is usually a monotonic decreasing function as calls further from a microphone are usually less detectable. Here, we use the signal strength detection function (Efford, Dawson & Borchers 2009; further detail provided in below), and this depends on the signal strength parameters  $\gamma$ . Assuming independence across microphones, the probability that a call made at  $x$  is detected at all is therefore  $p(x; \gamma) = 1 - \prod_{j=1}^k 1 - g(d_j(x); \gamma)$ , where  $d_j(x)$  is the distance between the location  $x$  and the  $j^{\text{th}}$  microphone. The ESA depends on the detection function and is given by  $a(\gamma) = \int_A p(x; \gamma) dx$  (Borchers & Efford 2008; Borchers 2012).

The average call rate of calling members of the population at the time of the survey,  $\mu_r$ , is estimated from a separate, independent sample of  $n_r$  call rates,  $r = (r_1, \dots, r_{n_r})$ . If  $r$  is used to estimate a parametric distribution for population call rates, then the vector  $\psi$  holds the associated parameters. The final parameter of interest is calling animal density,  $D_a$ .

Throughout this manuscript, we do not explicitly differentiate between a random variable and its observed value, instead this should be clear from its context. Likewise, we use the function  $f(\cdot)$  to generically denote any probability density function (PDF) or probability mass function (PMF) without explicit differentiation. The random variable(s) that  $f(\cdot)$  is associated with should be clear from its argument(s). From Equation (2) onwards, we omit the indexing of parameters in PDFs and PMFs for clarity.

CALL DENSITY ESTIMATOR

The estimator we propose for  $\theta$  is based on an SECR model, which we describe in this section.

The full likelihood is the joint density of the data collected from the acoustic survey, as a function of the model parameters:

$$L(\theta) = f(n_c, \Omega, Y, Z; \theta) = f(n_c; D_c, \gamma) f(\Omega, Y, Z | n_c; \gamma, \phi). \tag{eqn 1}$$

Note that  $D_c$  does not appear in the second term of Equation (1). This is a consequence of assuming that call density is constant over the survey area (Borchers & Efford 2008).

SECR approaches often assume that the number of animals detected is a Poisson random variable, as animal locations are considered a realization of a Poisson point process. Because we do not know how many unique individuals have been detected, the distribution of the random variable  $n_c$  is not known (indeed, it is certainly not a Poisson random variable if individuals call more than once, see Appendix S3). This issue is linked to the dependence of within-animal call locations; independence in call locations implies that said locations are a realization of a Poisson point process, but any dependence violates this.

We use the so-called *conditional likelihood* approach of Borchers & Efford (2008), which we extend here to include signal strength and

time-of-arrival information. This allows for estimation of  $\theta$  without any distributional assumption on  $n_c$ , by conditioning on  $n_c$  itself. Parameters  $\gamma$  and  $\phi$  can be estimated directly using this likelihood, which is the second term in Equation (1):

$$L_n(\gamma, \phi) = f(\Omega, Y, Z | n_c). \tag{eqn 2}$$

Once the estimate  $\hat{\gamma}$  has been obtained, an estimate of  $D_c$  can then be calculated using a Horvitz–Thompson-like estimator. This is accomplished by dividing the number of detected calls by the estimated ESA and the survey length, that is

$$\hat{D}_c = \frac{n_c}{a(\hat{\gamma})T}. \tag{eqn 3}$$

Estimates for SECR model parameters that are obtained via maximization of the full likelihood are in fact equal to those obtained via maximization of the conditional likelihood and use of a Horvitz–Thompson-like estimator (Borchers & Efford 2008), so there is no practical difference in the two approaches if we are only interested in point estimates (though note that this only holds when density is assumed constant across the survey area). Indeed, specifying the distribution for the number of detections (here denoted as  $n_c$ ) only serves to allow calculation of estimate uncertainty; here,  $\hat{D}_c$  depends on  $n_c$ , and so uncertainty in  $\hat{D}_c$  is subject to the variance of  $n_c$ .

Let us now describe the conditional likelihood, Equation (2), in further detail. The capture histories,  $\Omega$ , received signal strengths,  $Y$ , and times of arrival,  $Z$ , all depend on the call locations  $X$ : the closer a call is made to a microphone, the higher the probability of detection, the louder the expected received signal strength, and the earlier the expected measured time of arrival. We therefore obtain the joint density of  $\Omega, Y$  and  $Z$ , conditional on  $n_c$ , by marginalizing over  $X$ :

$$\begin{aligned} L_n(\gamma, \phi) &= \int_{A^{n_c}} f(\Omega, X, Y, Z | n_c) dX \\ &= \int_{A^{n_c}} f(\Omega, Y, Z | X, n_c) f(X | n_c) dX \\ &= \int_{A^{n_c}} f(Y, Z | \Omega, X, n_c) f(\Omega | X, n_c) f(X | n_c) dX. \end{aligned}$$

By assuming independence between the detected calls' recorded signal strengths and times of arrival, conditional on  $X$  (i.e. the time of a call's detection does not depend on its strength), we obtain

$$L_n(\gamma, \phi) = \int_{A^{n_c}} f(Y | \Omega, X, n_c) f(Z | \Omega, X, n_c) f(\Omega | X, n_c) f(X | n_c) dX.$$

The conditional likelihood presented above is intractable for two reasons: (i) in general, the joint density of the call locations,  $f(X | n_c)$ , is unknown as we are unable to allocate calls to individuals – the dependence between call locations is not known and (ii) the integral is of dimension  $2n_c$ , usually rendering any method of its approximation too computationally expensive to be feasible.

Instead, we compute the *simplified likelihood* that overcomes these two problems by treating call locations as if they are independent. Justification for this is that treating non-independent data as if they are independent often has minimal effect on the bias of an estimator (though variance estimates may be affected substantially). This gives  $f(X | n_c) = \prod_{i=1}^{n_c} f(x_i)$  and results in a separable integral, allowing for the evaluation of a product of  $n_c$  2-dimensional integrals instead of a single  $2n_c$ -dimensional integral:

$$L_s(\gamma, \phi) = \prod_{i=1}^{n_c} \int_A f(y_i | \omega_i, x_i) f(z_i | \omega_i, x_i) f(\omega_i | x_i) f(x_i) dx_i. \tag{eqn 4}$$



Estimates for  $\gamma$  and  $\phi$  are found by maximizing the log of the simplified likelihood function, that is

$$(\hat{\gamma}, \hat{\phi}) = \arg \max_{\gamma, \phi} \log(L_s(\gamma, \phi)), \quad \text{eqn 5}$$

and our estimator for  $D_c$  remains as shown in Equation (3).

In situations where call locations *can* be considered independent, the conditional and simplified likelihoods are equivalent. Otherwise, the simplified likelihood is not a true likelihood per se and should not be treated as such. That is, any further likelihood-based inference (such as the calculation of standard errors based on the curvature of the log-likelihood surface at the maximum likelihood estimate, or likelihood-based information criteria) should not be directly used.

The following sections focus on providing further details about each term that appears in the integrand of Equation (4).

### Signal strength

The use of signal strength to improve estimator precision in SECR models was first proposed by Efford, Dawson & Borchers (2009).

Assuming independence between received signal strengths (see the discussion for comments on this point), the first component of the integrand in Equation (4) is

$$f(\mathbf{y}_i | \boldsymbol{\omega}_i, \mathbf{x}_i) = \prod_{j=1}^k f(y_{ij} | \omega_{ij}, \mathbf{x}_i).$$

The expected received signal strength of the  $i^{\text{th}}$  call at the  $j^{\text{th}}$  microphone can be any sensible monotonic decreasing function of  $d_j(\mathbf{x}_i)$ , the distance between the  $j^{\text{th}}$  microphone and the location of the  $i^{\text{th}}$  call. Here, we simply use

$$E(y_{ij} | \mathbf{x}_i) = h^{-1}(\beta_{0s} - \beta_{1s} d_j(\mathbf{x}_i)),$$

where  $h^{-1}(\cdot)$  is the inverse of a link function (typically chosen to be either the identity or log function). See Dawson & Efford (2009) for alternative specifications of the expected signal strength. We account for Gaussian measurement error in the received signal strengths, that is  $y_{ij} | \mathbf{x}_i \sim N(E(y_{ij} | \mathbf{x}_i), \sigma_s)$ .

The parameter vector  $\gamma$  therefore comprises  $\beta_{0s}$ ,  $\beta_{1s}$  and  $\sigma_s$  that have direct signal strength interpretations:  $\beta_{0s}$  is the source signal strength of calls (on the link function's scale),  $\beta_{1s}$  is the loss of strength per metre travelled due to signal propagation (on the link function's scale), and  $\sigma_s$  is the standard deviation of the normal distribution used to account for signal measurement error.

However, recall that  $y_{ij}$  is only observed if the received signal strength exceeds the microphone threshold of detection, that is, if and only if  $y_{ij} > c$  (or, equivalently,  $\omega_{ij} = 1$ ). Otherwise,  $y_{ij}$  is discarded and  $\omega_{ij}$  is set to 0. Therefore, we set  $f(y_{ij} | \omega_{ij} = 0, \mathbf{x}_i)$  to 1, and  $(y_{ij} | \omega_{ij} = 1, \mathbf{x}_i)$  is a random variable from a truncated normal distribution, giving

$$f(y_{ij} | \omega_{ij} = 1, \mathbf{x}_i) = \frac{1}{\sigma_s} f_n \left( \frac{y_{ij} - E(y_{ij} | \mathbf{x}_i)}{\sigma_s} \right) \left( 1 - \Phi \left( \frac{c - E(y_{ij} | \mathbf{x}_i)}{\sigma_s} \right) \right)^{-1}, \quad \text{eqn 6}$$

where  $f_n(\cdot)$  and  $\Phi(\cdot)$  are the PDF and the cumulative density function of the standard normal distribution, respectively.

### Probability of detection

Based on the previous section, Efford, Dawson & Borchers (2009) proposed the *signal strength detection function*, to be used when signal strength information has been collected by the detectors during an

SECR survey. This takes the form

$$g(d; \gamma) = 1 - \Phi \left( \frac{c - h^{-1}(\beta_{0s} - \beta_{1s} d)}{\sigma_s} \right),$$

thus giving the probability of a call's received signal strength exceeding  $c$  (and, therefore, the probability of detection).

The  $i^{\text{th}}$  capture history,  $\boldsymbol{\omega}_i$ , is only observed if the  $i^{\text{th}}$  call is detected, that is if  $\sum_{j=1}^k \omega_{ij} > 0$ . Thus, we observe  $\boldsymbol{\omega}_i$  conditional on detection, and so  $f(\boldsymbol{\omega}_i | \mathbf{x}_i)$  must incorporate the probability of detection in the denominator. Assuming independent detections of each call across all microphones, the third component of the integrand in Equation (4) is therefore

$$f(\boldsymbol{\omega}_i | \mathbf{x}_i) = \frac{\prod_{j=1}^k f(\omega_{ij} | \mathbf{x}_i)}{p(\mathbf{x}_i; \gamma)}.$$

As  $\omega_{ij}$  is 1 if the  $i^{\text{th}}$  call is detected by the  $j^{\text{th}}$  microphone, and 0 otherwise, we have

$$f(\omega_{ij} | \mathbf{x}_i) = \begin{cases} g(d_j(\mathbf{x}_i); \gamma) & \omega_{ij} = 1, \\ 1 - g(d_j(\mathbf{x}_i); \gamma) & \omega_{ij} = 0. \end{cases} \quad \text{eqn 7}$$

### Time of arrival

A single detection time on its own is not informative on call location. It is only *differences* between precise arrival times that provide information about the relative position of a call in relation to the locations of the microphones at which it was detected. Time-of-arrival data are therefore only informative for calls detected at two or more microphones; the arrival times,  $z_i$ , depend on  $\boldsymbol{\omega}_i$  through  $m_i$ , the number of microphones that detected the  $i^{\text{th}}$  call, that is  $m_i = \sum_{j=1}^k \omega_{ij}$ ,  $m_i \in \{1, \dots, k\}$ . Therefore,  $f(\mathbf{z}_i | \boldsymbol{\omega}_i, \mathbf{x}_i) \equiv f(\mathbf{z}_i | m_i, \mathbf{x}_i)$ , and we set  $f(\mathbf{z}_i | m_i = 1, \mathbf{x}_i)$  to 1.

Information about call locations improves the precision of parameter estimates, though here we do not assume that times of arrival allow perfect triangulation of call locations. Instead, we account for uncertainty in recorded times of arrival due to Gaussian measurement error, controlled by the parameter  $\sigma_r$ . For calls detected at two or more microphones, inference can be made by marginalizing over the time the call was made, a latent variable, and this integral is available in closed form (see the online supplementary material of Borchers *et al.* in press),

$$f(\mathbf{z}_i | m_i > 1, \mathbf{x}_i) = \frac{(2\pi\sigma_r^2)^{(1-m_i)/2}}{2T\sqrt{m_i}} \exp \left( \sum_{\{j: \omega_{ij}=1\}} \frac{(\delta_{ij}(\mathbf{x}_i) - \bar{\delta}_i)^2}{-2\sigma_r^2} \right). \quad \text{eqn 8}$$

The term  $\delta_{ij}(\mathbf{x}_i)$  is the expected call production time, given call location  $\mathbf{x}_i$ , and the time of arrival collected by detector  $j$ , that is  $\delta_{ij}(\mathbf{x}_i) = z_{ij} - d_j(\mathbf{x}_i)/v$ , where  $v$  is the speed of sound. The average across all detectors on which a detection was made is  $\bar{\delta}_i$ .

### Call locations

We assume individuals' locations are a realization of a homogeneous Poisson point process across the survey area,  $A$ . As the dependence between call locations is not clear, it is not possible to specify their joint density,  $f(\mathbf{X})$ , from data collected by the acoustic survey alone. Under the simplified likelihood (Equation 4), this is now tractable:  $\mathbf{X}$  itself is a realization of a filtered homogeneous Poisson point process – the intensity of *emitted* calls is constant across the survey area, but the intensity of *detected* calls is highest closest to the microphones. The filtering is

therefore through the detection probability surface. We now have  $f(\mathbf{X}) = \prod_{i=1}^n f(\mathbf{x}_i)$ , and  $f(\mathbf{x}_i)$  is proportional to the intensity of the point process, that is  $f(\mathbf{x}_i) \propto p(\mathbf{x}_i; \gamma)$ . As  $a(\gamma) = \int_{AP} p(\mathbf{x}; \gamma) d\mathbf{x}$ , the ESA is the normalizing constant, and we obtain

$$f(\mathbf{x}_i) = \frac{p(\mathbf{x}_i; \gamma)}{a(\gamma)}.$$

We have now provided details for all terms in the integrand of the simplified likelihood, Equation (4).

### CALLING ANIMAL DENSITY ESTIMATOR

Although call density,  $D_c$ , may be informative in situations where a species' call rate is of primary interest, it is usually the density of calling individuals per unit area,  $D_a$  that is required.

First used in distance sampling by Hiby (1985), a common method used to obtain an estimate for calling animal density from call density involves dividing call density by the average call rate across the calling population, that is  $\hat{D}_a = \hat{D}_c / \hat{\mu}_r$  (see Buckland *et al.* 2001; pp. 191–197). See Appendix S2 for justification for this estimator from its asymptotic properties.

If  $\mu_r$  is not known *a priori*, then it must be estimated separately from call rate data,  $r$ , collected independently of the acoustic survey. In the simplest case, the sample mean  $\bar{r} = n_r^{-1} \sum_{i=1}^{n_r} r_i$  is an estimator for  $\mu_r$ . If the average call rate is known to vary (e.g. perhaps due to covariates such as rainfall, season or temperature), then it is important to observe  $r$  at the same time as the acoustic survey. Alternatively, given call rate data collected across a range of such covariates, a model could be fitted to estimate the average call rate for specific conditions of a future survey, thereby reducing future field effort.

In any case, for calculation of variance estimates (below), one has to simulate call rate data from whatever model is used to estimate  $\mu_r$ . In the case of taking a simple random sample of  $n_r$  call rates, this can be done using the empirical distribution function (EDF). Otherwise, if a parametric model has been fitted to  $r$  (potentially using covariates, as described above), then such data can be generated from  $f(r; \hat{\Psi})$ .

### THE BOOTSTRAP PROCEDURE

We calculate estimate uncertainty (i.e. standard errors and confidence intervals for the model parameters) using a parametric bootstrap. By combining parameter estimates calculated from the acoustic survey and the call rate data, we can simulate data in a way that mimics the real data generation process, including dependencies in call locations.

Here, we use the superscript  $*$  to denote simulated data or parameters estimated from simulated data. We propose the following algorithm:

1. Simulate animal locations as a realization of a homogeneous Poisson point process with intensity  $\hat{D}_a$ .
2. Determine the number of calls made by each individual by simulating call rates from either the EDF of  $r$  or  $f(r; \hat{\Psi})$ .
3. Generate  $\mathbf{X}^*$  by repeating each location from Step 1 the appropriate number of times, given by Step 2.
4. Obtain  $\Omega^*$  by simulating from  $f(\omega_{ij} | \mathbf{x}_i^*; \hat{\gamma})$  (Equation (7)). Omit all rows from  $\Omega^*$  and  $\mathbf{X}^*$  that are associated with undetected calls.
5. Obtain  $\mathbf{Y}^*$  by simulating from  $f(y_{ij} | \omega_{ij}^* = 1, \mathbf{x}_i^*; \hat{\gamma})$  (Equation (6)) and  $\mathbf{Z}^*$  by simulating from  $f(z_i | \omega_i^*, \mathbf{x}_i^*; \hat{\phi})$  (Equation (8)) for all detections.
6. Calculate  $\hat{\theta}^*$  from  $\Omega^*$ ,  $\mathbf{Y}^*$  and  $\mathbf{Z}^*$  using Equations (3) and (5).
7. Obtain  $r^*$  by simulating from either its EDF or  $f(r; \hat{\Psi})$ , calculate  $\hat{\Psi}^*$  and therefore  $\hat{\mu}_r^*$ .
8. Calculate  $\hat{D}_a^* = \hat{D}_c^* / \hat{\mu}_r^*$ .

9. Repeat the above steps  $R$  times and save the parameter estimates from each iteration.

Here, we treat  $D_a$  as the sole parameter of interest, but in practice, the following holds for any other estimated parameter. Let the saved density estimates from the simulated data be  $\hat{D}_a^* = (\hat{D}_{a1}^*, \hat{D}_{a2}^*, \dots, \hat{D}_{aR}^*)$ . Bias can be estimated by subtracting the parameter estimate from the mean of the estimates from the bootstrap samples (Davison & Hinkley 1997), that is  $\bar{D}_a^* - \hat{D}_a$ , where  $\bar{D}_a^* = R^{-1} \sum_{i=1}^R \hat{D}_i^*$ .

Confidence intervals can be calculated using any suitable bootstrap confidence interval method, many of which are outlined by Davison & Hinkley (1997). The simplest approach is to calculate confidence intervals based on a normal approximation, using  $SD(\hat{D}_a^*)$  as the standard error. Note that the normal approximation may be more suitable for a transformation of  $\hat{D}_a$  (e.g.  $\log(\hat{D}_a)$ ), and so a back-transformation of a confidence interval based on this transformed parameter may have better coverage properties. Other possible approaches include the so-called *basic* and *percentile* methods, although note that the latter requires  $R$  to be larger in comparison with the normal approximation and basic methods.

Note that Step 5 above makes the assumption that individuals do not move over the course of the survey. See the discussion for comments on accounting for animal movement.

### APPLICATION TO ARTHROLEPTELLA LIGHTFOOTI

We use the method presented above to generate estimates of call and calling male density of *A. lightfooti*, and estimate associated variances.

#### Equipment and survey design

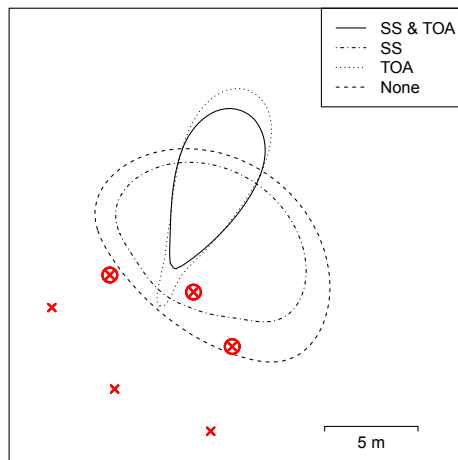
The data we use were generated from a 25-s subset of a recording carried out on 16 May 2012.

The recording was made using an array of six Audio-Technica AT8004 handheld omni-directional dynamic microphones, connected to a DR-680 8-Track portable field audio recorder via Hosa Technology STX-350F Professional 1/4 inch TRS male to XLR female cables. Each of the six microphones were placed in microphone holders which were fastened atop 1-m-tall wooden dowels. The immediate vicinity was vacated during the recording. The configuration of our array is shown in Fig. 1

#### Acoustic pre-processing

The open-source software package PAMGUARD (Gillespie *et al.* 2009; see [www.pamguard.org](http://www.pamguard.org)) was used in order to identify calls of *A. lightfooti* males, which have a signature frequency of 3.8 kHz. The first 600 s of the recording were ignored in case any disturbance to the frogs during set-up affected calling behaviour. Furthermore, a detection was only recorded if the strength of the received signal was above a threshold of 130 units. Along with signal strengths, precise times of signal arrival (accurate to  $2.083 \times 10^{-5}$  s) were also recorded for each detection.

In order to construct the observed  $\Omega$ ,  $\mathbf{Y}$  and  $\mathbf{Z}$ , it was necessary to determine which detected sounds on different microphones were of the same call from the same frog. As individuals are not recognizable from their calls, this was done as follows: if two calls were detected within  $d/330$  seconds of one another by two microphones that were  $d$  metres apart, then they are assumed to have the same source (using  $330 \text{ ms}^{-1}$  as the speed of sound in air).



**Fig. 1.** Estimated locations of a detected call from SECR models with various levels of supplementary information. Crosses show the microphone locations, while circled crosses indicate the microphones at which this particular call was detected. Each contour shows the area within which the call was estimated to have originated with a probability of 0.9. As more additional data are used, the area inside the contour decreases, representing a more precise location estimate.

Note that this approach to call identification will never result in detections of the same call being attributed to different frogs; however, there is potential for calls from different frogs to be falsely identified as the same individual. This is unlikely, however, as calls from males are temporally negatively correlated; they tend to call in turn in an attempt to increase their likelihood of being heard by a female (Altwegg & Measey, pers. obs.).

### Bootstrap details

No individual call rate data were collected concurrently with the acoustic survey. Instead, we use call rate data collected at another time and location so that we are able to demonstrate the methods described above. Call rate data were obtained by finding locations of 8 individual calling males and placing a microphone in close proximity; this ensured that all calls they emitted were detected and were easily identifiable from calls of other males.

We ran the bootstrap procedure for 10 000 iterations in order to reduce the relative Monte Carlo error associated with the standard error (calculated using equation (9) in Koehler, Brown & Haneuse 2009) to below 1%.

### SIMULATION STUDY

We test our method using a simulation study. A total of 1000 data sets were independently simulated using Steps 1–5 and Step 7 from the bootstrap procedure. Values used for the simulation parameters were set at the corresponding estimates obtained from the real data analysis. For each simulated data set, we use the method we outline above to obtain both point estimates and confidence intervals for  $D_a$  and  $D_c$ . We used 500 bootstrap repetitions for each iteration in order to prevent the simulation from being prohibitively time-consuming. For comparison, we also calculate confidence intervals based on the approach of Efford, Dawson & Borchers (2009), which ignores the dependence between call locations.

We also conduct a simulation study to investigate the impact of using time-of-arrival information in addition to the signal strength data. A total of 10 000 data sets were independently simulated, the same way

as above, and two estimates of both  $D_a$  and  $D_c$  were obtained from each: one from a model that used time-of-arrival information and another from a model that did not.

### SOFTWARE IMPLEMENTATION

Implementation of the methods we present was accomplished using the R package `admbsecr` (Stevenson & Borchers 2014; see <https://github.com/b-steve/admbsecr>). This software can be used to obtain parameter estimates via numerical maximization of the log of the simplified likelihood. Optimization is carried out by a call to an executable generated by AD Model Builder (Fournier *et al.* 2012). Numerical integration is used to approximate marginalization over call locations.

The code used to carry out analysis of the *A. lightfooti* data can be found in Appendix S1

## Results

### REAL DATA ANALYSIS

A total of 225 unique calls were detected by the six microphones over the course of the 25-s survey.

Density parameter estimates, their associated standard errors and estimated biases (obtained from the bootstrap procedure) are provided in Table 1. We use  $\hat{\gamma}$  to plot the detection function, shown in Fig. 2. To illustrate the utility of the time-of-arrival information, we plot uncertainty surrounding the estimation of a location of one of the detected calls in Fig. 1.

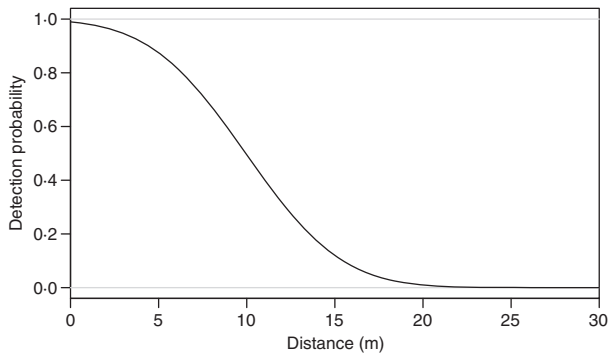
Normal QQ plots for  $\hat{D}_a^*$  and  $\hat{D}_c^*$  both indicated approximate normality, and so confidence intervals based on a normal approximation using the standard errors shown in Table 1 were deemed to be appropriate. Setting the nominal coverage at 95%, this approach gave an interval of (239.42, 492.75) for  $D_a$  and an interval of (65.06, 133.23) for  $D_c$ ;  $D_a$  is calling males per hectare and  $D_c$  is calls per hectare per second.

### SIMULATION STUDY

We show the performance of a number of confidence interval calculation methods in Table 2. Coverage is only significantly different (at the 5% level) to the nominal 95% coverage rate for both intervals calculated using the basic bootstrap method, and for naïve confidence intervals that rely on call locations being independent (as per the method of Efford, Dawson & Borchers 2009).

**Table 1.** Parameter estimates, standard errors and estimated biases from analysis of the *Arthroleptella lightfooti* data.  $D_c$  is in calls per hectare per second,  $D_a$  is in calling males per hectare,  $\sigma_t$  is in milliseconds, and  $\mu_r$  is in calls per individual per 25 s

Parameter	Estimate	Standard error	Bias (%)
$D_c$	99.15	17.39	0.59
$\beta_{0s}$	156.57	1.81	-0.14
$\beta_{1s}$	2.67	0.18	-0.22
$\sigma_s$	11.50	0.44	-0.07
$\sigma_t$	1.96	0.12	0.60
$D_a$	366.08	64.63	0.62
$\mu_r$	6.77	0.12	0.01



**Fig. 2.** Estimated detection function,  $g(d; \hat{\gamma})$ , from the *Arthroleptella lightfooti* data.

Estimates of bias, variance and mean square error of the estimators investigated in the second simulation study are shown in Table 3. The estimator that utilizes time-of-arrival data is more precise and less biased. Estimated sampling distributions of the estimates obtained both with and without the time-of-arrival information are shown in Fig. 3.

**Discussion**

**SUMMARY**

The method we have proposed to estimate calling animal density from a fixed microphone array relies on maximizing a simplified likelihood (Equation 4). We then use a parametric bootstrap to account for dependence between call locations.

In our simulation studies, parameter estimates were shown to have negligible bias (in all cases, bias was estimated at substantially less than 1% of the estimate sizes; see Tables 1 and 3). Note that this is despite the simplified likelihood treating call locations as independent. Our findings suggest that density estimates obtained via acoustic SECR methods are robust to this violation. The bootstrap confidence interval methods generated intervals with coverage close to their nominal level (Table 2). Indeed, these easily outperformed the method that does not account for dependence among call locations in the construction of confidence intervals.

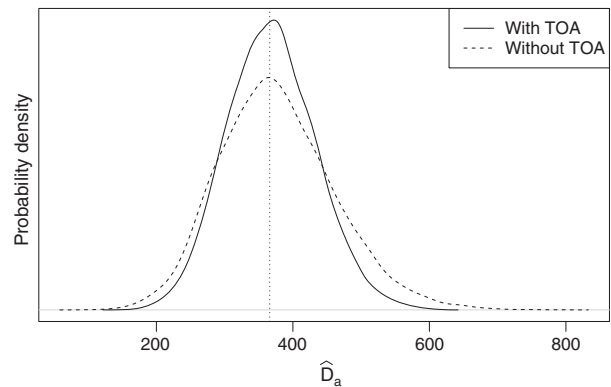
Using time-of-arrival information led to decreased bias and substantially increased precision in density estimates (Fig. 3, Table 3) in comparison with the approach of Efford, Dawson & Borchers (2009). In applications like ours, time-of-arrival data are far more informative on animal location than trap

**Table 2.** Coverage of various confidence interval methods for the parameters  $D_a$  and  $D_c$ . Nominal coverage was set at 95%. The basic, normal, and percentile methods rely on the bootstrap procedure. The naïve method assumes independence between call locations and cannot be used to calculate a confidence interval for  $D_a$

CI method	$D_a$	$D_c$
Basic	0.924	0.927
Normal	0.942	0.941
Percentile	0.942	0.946
Naïve	–	0.729

**Table 3.** Performance of  $D_a$  estimators with and without the use of time-of-arrival data. Calculated bias is  $\hat{E}(\hat{D}_a - D_a)$  as a percentage of  $D_a$ . CV gives the coefficient of variation as a percentage. MSE gives the mean square error. The simulated data were generated with  $D_a$  set at 366.08

Estimator	Bias (%)	CV (%)	MSE
With TOA	0.62	17.65	4181.73
Without TOA	2.93	23.08	7256.95



**Fig. 3.** Estimated sampling distributions of  $\hat{D}_a$  for models with and without time-of-arrival information incorporated. The dotted vertical line shows the value of  $D_a$  used to generate the simulated data.

location and signal strength information (Fig. 1). With more information on where calls are located, the detection function parameters can be estimated more precisely. In turn, this results in higher precision estimates of the ESA, call density and calling animal density.

**ANIMAL MOVEMENT**

The approach we present here assumes that calls made by the same individual are associated with the same location, which is a reasonable assumption for our case study of *A. lightfooti*. A natural extension is to account for animal movement. We outline two ways of doing this here.

The first is to adjust our bootstrap method. This requires the fitting of a movement model (e.g. Jonsen, Flemming & Myers 2005; McClintock *et al.* 2012; see King 2014; for an overview) to independently collected data, explaining between-call animal movement patterns. Rather than the bootstrap procedure allocating all calls to the same location, movement can be introduced using parameter estimates from the movement model, resulting in appropriate variance estimates. However, we recognize that this may represent an infeasible amount of field effort in addition to the acoustic survey.

If individuals can be identified from their calls, then the analysis of Ergon & Gardner (2013) suggests an alternative way forward. A new SECR approach was used to analyse live-trapping data of field voles *Microtus agrestis* (Linnaeus), where individuals' home range centres moved (due to a dispersion model) from one survey session to the next. Similar approaches could possibly be used to account for animal movement in acoustic SECR



surveys. There are complications, however, associated with detections in continuous time rather than allowing movement across discrete sessions: one must integrate over all possible paths an individual could have taken between detection occasions, considerably increasing computational complexity.

#### INFERENCE VIA THE CONDITIONAL LIKELIHOOD

It would be beneficial to propose estimators based on the maximization of the conditional likelihood (Equation 2) rather than the simplified likelihood (Equation 4). Such an approach would deal directly with call location dependence, removing the need to collect data or make restrictive assumptions about call rates and animal movement. Under a classical framework, this would also result in maximization of a true likelihood, allowing for use of further likelihood-based inference.

It is not clear how this could be achieved when animal identification is not possible; a solution to this so-called *unknown identification problem* would present a significant breakthrough. One possible approach is to use a reversible jump Markov chain Monte Carlo procedure under a Bayesian framework. The number of unique detected individuals, as well as the allocations of calls to individuals, would vary from iteration to iteration. Alternatively, inference could potentially be made using methods that deal with the estimation of parameters from intractable likelihoods (e.g. the synthetic likelihood approach of Wood 2010).

Otherwise, if animal identities *can* be determined, possible methods of incorporating animal movement and call rate into the conditional likelihood are a little clearer. The dependence between latent locations of calls from the same individual is obvious under the assumption of no animal movement, and potentially estimable via a movement model otherwise.

Direct estimation of the average call rate,  $\mu_r$  (and therefore calling animal density), is also likely to be possible from the acoustic survey. In order to obtain this, one must specify a distribution with mean  $\mu_r$  for the number of calls made by individuals to account for the call production process. This is then filtered by the detection process, giving rise to the observed data and call identities.

#### FURTHER GENERALIZATIONS

Our method is more general than that of Efford, Dawson & Borchers (2009), as we do not rely on assumptions regarding independence of call locations for variance estimation. Further generalizations are possible, and we outline two of them here. First, our method assumes that individuals all emit calls with the same strength,  $\beta_{0s}$ , which may not hold. Secondly, there is the issue of directional calling: the orientation of an individual may result in the loss of strength per metre,  $\beta_{1s}$ , due to signal propagation at a lower rate in some directions. Our method assumes signal propagation occurs uniformly across all directions.

It is likely that further latent variables will be required to fit models appropriate for either case, that is latent call source strengths or latent individual orientations, respec-

tively. With additional latent variables comes further computational complexity: under a classical framework, these must be integrated out of the likelihood. A Bayesian approach presents a viable alternative; latent variables can be sampled from rather than marginalized over, which is potentially simpler.

#### SPATIOTEMPORAL CHANGES IN DENSITY

In some situations, it is not necessarily animal density that is of particular ecological interest, but rather temporal or spatial variation in density. Our method can be used to make inference in either case. Independent microphone arrays set out at various points in time and space will generate separate density estimates, from which temporal and spatial shifts of animal abundance can be determined.

There is also potential for an alternative: in general, SECR methods are capable of directly estimating a density intensity *surface*, rather than a constant intensity over the survey area. We have skirted this issue for brevity; assuming a constant density is reasonable in many cases over small survey areas.

#### ANALYSIS OF *ARTHROLEPTELLA LIGHTFOOTI* DATA

Regarding the survey of *A. lightfooti*, our method obtained an estimate of 366.08 calling males per hectare. Alternative methods used to monitor abundance of threatened species in the genus *Arthroleptella* make use of auditory estimates (Measey *et al.* 2011). Trained practitioners stand at a set locale and listen to an assemblage, placing call abundance into a category (Dorcas *et al.* 2009); the assemblage calling in this study was assessed using this method, falling into the highest category, >100 individuals. It is difficult to compare the two estimates as this abundance cannot be converted into a density.

Our estimates of call density and calling male density are associated with coefficients of variation of approximately 17.5% from just 25 s worth of recording using only six microphones (Table 1). The relatively high precision of  $\hat{D}_a$  is in part due to the fact that variance in the recorded call rates,  $r$ , was very low as individual *A. lightfooti* call at very regular intervals. This allowed for a precise estimate of  $\mu_r$  which was used in the calculation of  $\hat{D}_a$ . Uncertainties associated with our density estimators decrease as survey length and  $n_r$  increase (see Appendix S2, fig. 1).

#### CONCLUDING REMARKS

Our method advances acoustic SECR methodology by improving estimator precision via time-of-arrival information and by proposing an unbiased estimator for calling animal density. Our confidence intervals account for dependence in call locations, which had previously been ignored. Our analysis here is the first to provide reliable point and interval estimates of both the call and calling male density of a frog species from an acoustic survey. This approach is general and can be applied to estimate calling animal density for a wide variety of species.

## Acknowledgements

We thank both Tanya Scott and Paula Strauss for their assistance in the field.

Data collection was made possible due to access facilitated by CapeNature (Permit No. AAA007-00084-0035) and South African National Parks (Table Mountain National Park).

Funding for the frog survey was received from the National Geographic Society/Waite Grants Program (No. W184-11). The EPSRC and NERC helped to fund this research through a PhD grant (No. EP/1000917/1).

B.C.S. wishes to acknowledge the Auckland Grammar School board of trustees for further financial assistance through the F.W.W. Rhodes Scholarship.

G.J.M. would like to thank the South African National Biodiversity Institute and the DST-NRF Centre of Excellence for Invasion Biology.

We are grateful to two anonymous reviewers, whose comments lead to substantial improvements to the content and structure of this manuscript.

## Data accessibility

The data used in this manuscript are already available as exported data in the R package `admbsecr`: <https://github.com/b-steve/admbsecr>.

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Received 7 June 2014; accepted 7 October 2014  
Handling Editor: Robert Freckleton

## Supporting Information

Additional Supporting Information may be found in the online version of this article.

**Appendix S1.** R code.

**Appendix S2.** Animal density estimator.

**Appendix S3.** Distribution of the detected call count.